

12.THERMODYNAMICS

Single Correct Answer Type

- A gas does 4.5 J of external work during adiabatic expansion. If its temperature falls by 2K, its internal 1. energy will
 - a) Increase by 4.5 J b) decrease by 4.5 J c) decrease by 2.25 J d) Increase by 9.0 J
- Two different adiabatic paths for the same gas intersect two isothermals at T_1 and T_2 as shown in the 2. P - V diagram (Fig). Then

 $V_{a}V_{d}$ a

$$)\frac{V_a}{V_c} = \frac{V_b}{V_d} \qquad b)\frac{V_a}{V_b} = \frac{T_2}{T_1} \qquad c)\frac{V_a}{V_b} = \frac{V_d}{V_c} \qquad d)\frac{V_a}{V_d} = \frac{T_1}{T_2}$$

- 3. For a gas, the difference between the two specific heats is $4150 \text{ J kg}^{-1}\text{K}^{-1}$ and the ratio of the two specific heats is 1.4. What is the specific heat of the gas at constant volume in units of J kg⁻¹K⁻¹? b) 5186 c) 1660 a) 8475 d) 10375
- Three moles of an ideal gas are taken through a cyclic process *ABCA* as shown on T V diagram in Fig. 4. The gas loses 2510 J of heat in the complete cycle. If $T_A = 100$ K and $T_B = 200$ K, The work done by the gas during the process BC is **m ≜**

$$T_{C}$$

$$T_{B}$$

$$T_{A}$$

$$V_{A} = V_{C}$$

$$V_{B}$$

V

c) 4000 J

- a) 5000 J b) -5000 J d) -2500 J 5. A thermally insulated rigid container contains an ideal gas at 27°C. It is fitted with a heating coil of resistance 50 Ω . A current is passed through the coil for 10 minutes by connecting it to a d. c. source of 10 V. The change in the internal energy is a) Zero b) 300 J c) 600 J d) 1200 I
- A Carnot's engine whose sink is at a temperature of 300 K has an efficiency of 40%. By how much should 6. the temperature of the source be increased so as to increase the efficiency to 60%? a) 250 K b) 275 K c) 300 K d) 325 K
- Two monoatomic ideal gases 1 and 2 of molecular masses, M_1 and M_2 respectively are enclosed in 7. separate containers kept at the same temperature. The ratio of the speed of sound in gas 1 to that in gas 2 is

a)
$$\sqrt{\frac{M_1}{M_2}}$$
 b) $\sqrt{\frac{M_2}{M_1}}$ c) $\frac{M_1}{M_2}$ d) $\frac{M_2}{M_1}$

Figure shows a cyclic process *ABCA* in the V - T diagram. Which of the diagrams shown in Fig. shows the 8. same process on a P - V diagram



18. P - V plots for two gases during adiabatic processes are shown in Fig. Plots 1 and 2 should correspond respectively to

 $\begin{bmatrix} & & & \\ & & & \\ & & & & \\ & & & & \end{bmatrix}$

Þ

b) 0₂ and He c) He and Ar d) O_2 and N_2 a) He and O_2 19. A balloon is filled with a mixture of ideal gases. The pressure *P* in the balloon is related to the volume *V* as $PV^{2/3} = k$, where k is a constant. If T is the temperature of the mixture, volume V is proportional to b) *T*² c) *T*³ d) *T*⁴ a) T 20. A certain amount of heat energy is supplied to a monoatomic ideal gas which expands at constant pressure. What fraction of the heat energy is converted into work? c) $\frac{2}{5}$ b) $\frac{2}{3}$ d) $\frac{5}{7}$ a) 1

21. A thermodynamic process is shown in Fig. The pressures and volumes corresponding to some points in the figure are, $P_A = 3 \times 10^4 \text{Pa}$, $V_A = 2 \times 10^{-3} \text{m}^3$, $P_B = 8 \times 10^4 \text{Pa}$, $V_D = 5 \times 10^{-3} \text{m}^3$. In process *AB*, 600 J of heat and in process *BC*, 200 J of heat is added to the system. The change in the internal energy in process *AC* would be



a) 560 J b) 800 J c) 600 J d) 640 J 22. A vessel contains 1 mole of O_2 gas (molar mass 32) at a temperature *T*. The pressure of the gas is *P*. An identical vessel containing one mole of He gas (molar mass 4) at a temperature 2 *T* has a pressure of a) $\frac{P}{8}$ b) *P* c) 2*P* d) 8*P*

- 23. The internal energy of 3 moles of hydrogen at temperature *T* is equal to the internal energy of *n* moles of helium at temperature *T* / 2. The value of *n* is (assume hydrogen and helium to behave like ideal gases) a) 5 b) 10 c) $\frac{3}{2}$ d) 6
- 24. Figure shows a cyclic process. When a given mass of a gas is expanded from state *A* to state *B*, it absorbs 30J of heat energy. When the gas is adiabatically compressed from state *B* to state *A*, the work done on the gas is 50 J. The change in internal energy of the e gas in the process $A \rightarrow B$ is



a) 80 J
b) 20 J
c) -20 J
d) -50 J

25. During an adiabatic process, the pressure of a gas is proportional to the cube of its absolute temperature. The value of C_n/C_v for that gas is:

a)
$$\frac{3}{5}$$
 b) $\frac{4}{3}$ c) $\frac{5}{3}$ d) $\frac{3}{2}$

26. A monoatomic ideal gas, initially at temperature T_1 , is enclosed in a cylinder fitted with a frictionless piston. The gas is allowed to expand adiabatically to a temperature T_2 by releasing the pison suddenly. If

 L_1 and L_2 are the lengths of the gas column before and after expansion respectively, then T_1/T_2 is given by a) $\left(\frac{L_1}{L}\right)^{2/3}$ d) $\left(\frac{L_2}{L_1}\right)^{2/3}$ b) $\frac{L_1}{L_2}$ c) $\frac{L_2}{L_4}$ 27. In a given process on an ideal gas, dW = 0 and dQ < 0. Then for the gas b) The volume will increase a) The temperature will decrease c) The pressure will remain constant d) The temperature will increase 28. Two cylinders *A* and *B* fitted with pistons contain equal amounts of an ideal diatomic gas at 300 K. The piston of A is free to move, while that of B is held fixed. The same amount of heat is given to the gas in each cylinder. If the rise in temperature of the gas in A is 30 K, then the rise in temperature of the gas in B is a) 30 K b) 18 K c) 50 K d) 42 k 29. Two identical containers A and B fitted with frictionless pistons contain the same idal gas at the same temperature and the same volume V. The mass of the gas in A is m_A and that in B is m_B . The gas in each cylinder is now allowed to expand isothermally to the same final volume 2V. The changes in pressure in A and *B* are found to be ΔP and 1.5 ΔP respectively. Then b) $2 m_A = 3 m_B$ d) 9 $m_A = 4 m_B$ a) $4 m_A = 9 m_B$ c) $3 m_A = 2 m_B$ 30. The equation of state corresponding to 8 g of O₂ is (assume O₂ to be an ideal gas) a) PV = 8 RT b) $PV = \frac{RT}{4}$ c) PV = RT d) $PV = \frac{RT}{2}$ 31. Starting with the same initial conditions, an ideal gas expands from volume V_1 to V_2 in three different ways. The work done by the gas is W_1 if the process is purely isothermal, W_2 if purely isobaric and W_3 if purely adiabatic. Then b) $W_2 > W_3 > W_1$ c) $W_1 > W_2 > W_3$ d) $W_1 > W_3 > W_2$ a) $W_2 > W_1 > W_3$ 32. Two moles of ideal helium gas are in a rubber balloon at 30°C. The balloon is fully expandable and can be assumed to require no energy in its expansion. The temperature of the gas in the balloon is slowly changed to 35°C. The amount of heat required in raising the temperature is nearly (take $R = 8.31 \ I/mol. K$) a) 62/ b) 104/ c) 124/ d) 208/ 33. A closed hollow insulated cylinder is filled with gas at 0°C and also contains an insulated piston of negligible weight and negligible thickness at the middle point. The gas on one side is heated to 100°C. If the piston moves through 5 c m, the length of the follow cylinder is a) 13.65 cm b) 27.3 cm c) 38.6 cm d) 64.6 cm 34. The isothermal Bulk modulus of an ideal gas at pressure *P* is b) γ*P* d) P/γ a) P c) P/2 35. If the ratio $C_p/C_v = \gamma$, the change in internal energy of the mass of a gas, when the volume changes from V to 2 V at constant pressureP is c) $\frac{PV}{(\gamma-1)}$ d) $\frac{\gamma PV}{(\gamma - 1)}$ a) $\frac{R}{(\gamma - 1)}$ b) *PV* 36. The equation of state of a gas is $\left(P + \frac{aT^2}{V}\right) \times V^c = (RT + b)$ Where *a*, *b*, *c* and *R*are constants. The isotherms can be represented by $P = AV^m - BV^n$ Where A and B depend only on temperature and c) m = -c, n = 1a) m = -c, n = -1b) m = c, n = 1d) m = c, n = -1

37. Heat energy absorbed by a system in going through a cyclic process shown in Fig. is



- 47. Entropy of a thermodynamic system does not change when the system is used for
 - a) Conduction of heat from a hot reservoir to a cold reservoir
 - b) Conversion of heat into work adiabatically
 - c) Conversion of heat into internal energy isochorically
 - d) Conversion of work into heat isothermally
- 48. When an ideal monoatomic gas is heated at constant pressure, the fraction of heat energy supplied which increases the internal energy of the gas is
 - a) $\frac{2}{5}$ b) $\frac{3}{5}$ c) $\frac{3}{7}$ d) $\frac{3}{4}$
- 49. An ideal monoatomic gas is taken round the cycle *ABCA* as shown in the Fig. The work done during the cycle is



- b) 3 PV
 c) 6 PV
 d) 9 PV
- 50. The temperature of *n* moles of an ideal gas is increased from *T* to 3*T* in a process in which the temperature changes with volume as $T = kV^2$ where *k* is a constant. The work done by the gas in this process is

a)
$$n R T$$
 b) $2 n R T$ c) $\frac{3}{2} n R T$ d) $3 n R T$

51. A given mass of a gas expands from state *A* to *B* by three different paths 1, 2 and 3 as shown in Fig. If W_1, W_2 and W_3 respectively be the work done by the gas along the three paths, then



a) $W_1 > W_2 > W_3$ b) $W_1 < W_2 < dU + dW = 0$ is valid for

- b) $W_1 < W_2 < W_3$ c) $W_1 = W_2 = W_3$ d) $W_1 < W_2; W_1 < W_3$
- 52. *dU+dW*=0 is valid for
 a) Adiabatic process
 b) Isothermal process
 c) Isobaric process
 d) Isochoric process
 53. If heat energy Δ*Q* is supplied to an ideal diatomic gas, the increase in internal energy is Δ*U* and the work done by the gas is Δ*W*. The ratio Δ*Q*: Δ*U*: Δ*W* is
 - a) 5:3:2 b) 5:2:3 c) 7:5:2 d) 7:2:5
- 54. A Carnot's engine working between 300 K and 600 K has a work output of 800 J per cycle. How much heat
energy is supplied to the engine from the source in each cycle?a) 1400 Jb) 1500 Jc) 1600 Jd) 1700 J

Multiple Correct Answers Type

55. Figure shows the P - V diagram of a cyclic process *ABCA*



a) Work done in process $A \rightarrow B$ is 0.036 J

b) Work done in process $B \rightarrow C$ is -0.024 J

- c) Work done in process $C \rightarrow A$ is zero
- d) Work done in cycle *ABCA* is 0.06 J
- 56. An ideal gas is taken through a cyclic thermodynamic process involving four steps. The amounts of heat involved in these steps are $Q_1 = 5960$ J, $Q_2 = -5585$ J, $Q_3 = -2980$ J, and $Q_4 = 3645$ J respectively. The corresponding amounts of work done are $W_1 = 2200$ J, $W_2 = -825$ J and $W_3 = -1100$ J, and W_4 respectively. The efficiency of the cycle is η . Then

a) $W_4 = 765 J$ b) $W_4 = 275 J$ c) $\eta \simeq 11\%$ d) $\eta \simeq 16\%$

57. A gas undergoes a change in its state from position *A* to position *B via* three different paths as shown in figure. Select the correct statement

- a) Heat is absorbed by the gas in all the three paths
- b) Heat absorbed/released by the gas is maximum in path 1
- c) Temperature of the gas increases first and then decreases continuously in path 1
- d) Change in internal energy of the gas is same along all the three paths
- 58. *n* moles of an ideal monoatomic gas is kept in a closed vessel of volume 0.0083 m³ at a temperature of 300 K and a pressure of 1.6×10^6 Pa. Heat energy of 2.49×10^4 J is supplied to the gas. Given R = 8.3 J mol⁻¹K⁻¹
 - a) The value of n = 5

b) For the gas $C_p = 20.75 \text{ J mol}^{-1} \text{K}^{-1}$

c) The final temperature of the gas is 402°C

d) The Final pressure of the gas is 3.6 \times 10 6 Pa

- 59. If ΔQ represents the heat energy supplied to a system, ΔU the increase in internal energy and ΔW the work done by the system, then which of the following are correct?
 - a) $\Delta Q = \Delta W$ for an isothermal process b) $\Delta U = -\Delta W$ for an adiabatic process
 - c) $\Delta U = \Delta Q$ for an isochoric process d) $\Delta U = -\Delta Q$ for an isobaric process
- 60. An ideal gas is undergoing an adiabatic change. Which of the following pressure-temperature relations is true?

a) $p\gamma^{-1}T^{\gamma} = \text{constant}$ b) $p\gamma T^{1-\gamma} = \text{constant}$ c) $p\gamma T^{1-\gamma} = \text{constant}$ d) $p^{1-\gamma}T^{\gamma} = \text{constant}$ 61. Figure is the P - V diagram for a Carnot cycle. In this diagram,



- a) Curve AB represents isothermal process and BC adiabatic process
- b) Curve AB represents adiabatic process and BC isothermal process
- c) Curve *CD* represents isothermal process and *DA* adiabatic process
- d) Curve *CD* represents adiabatic process and *DA* isothermal process

62. An ideal gas is taken from the state A(p, V) to the state B(p/2, 2V) along a straight line path as shown in figure. select the correct statement from the following



Work done by the gas in going from *A* to *B* exceeds the work done in going from *A* to *B* under a) isothermal conditions

- b) In the T V diagram, path AB would become a parabola,
- c) In the p T diagram, path AB would be part of hyperbola
- d) In going from A to B, the temperature T of gas first increases to a maximum value 1 and then decreases 63. An ideal gas has pressure *P*, volume *V* and temperature *T*. The ratio $C_p/C_v = \gamma$ and *U* is the internal
 - energy. If R is the gas constant, then

a)
$$C_v = \frac{R}{\gamma - 1}$$
 b) $U = nC_v T$ c) $U = \frac{PV}{(\gamma - 1)}$ d) $U = nC_p T$

64. The initial state of *n* moles of an ideal gas is represented by P_1 , V_1 , T_1 and the final state by P_2 , V_2 , T_2 . W_i is the work done by the gas in an isothermal process ($T_1 = T_2 = T$) and W_a in an adiabatic process, then

a)
$$W_i = nRT \log_e \left(\frac{V_2}{V_1}\right)$$

b) $W_i = nRT \log_e \left(\frac{P_1}{P_2}\right)$
c) $W_a = \frac{1}{(\gamma - 1)} (P_1 V_1 - P_2 V_2)$
d) $W_a = \frac{nR}{(\gamma - 1)} (T_1 - T_2)$

65. An ideal gas having initial pressure P, volume V and temperature T is allowed to expand adiabatically until its volume becomes 5.66 V while its temperature falls to T/2. If f is the number of degree of freedom of gas molecules and W is the work done by the gas during the expansion, then

a)
$$f = 3$$
 b) $f = 5$ c) $W = \frac{5PV}{4}$ d) $W = \frac{3PV}{2}$

66. Which of the following is equation of state for an adiabatic process? c) $TV^{\gamma-1}$ constant d) $T^{\gamma}/p^{\gamma-1} = \text{constant}$ a) $pV^{\gamma} = \text{constant}$ b) $p/\rho^{\gamma} = \text{constant}$

67. An ideal gas is taken from state A (pressure P, volume V) to state B (pressure P/2, volume 2V) along a straight line in the P - V diagram as shown in fig. Then

The work done by the gas in the process A to B exceeds the work that would be done by it if the system a) were taken from A to B along the isotherm

- b) In the *T*-*V* diagram, the path *AB* becomes a part of a parabola
- c) In the *P*-*T* diagram, the path *AB* becomes a part of a hyperbola
- d) In going from A to B, the temperature T of the gas first increases to a maximum and then decreases
- 68. During the melting of a slab of ice at 273 K at atmospheric pressure
 - a) Positive work is done by ice-water system on the atmosphere
 - b) Positive work is done on the ice-water system by the atmosphere
 - c) The internal energy of the ice-water system increases
 - d) The internal energy of the ice-water system decreases

fusion of ice is 80 cal/g

- a) Heat extracted from water is 3.36×10^5 J
- b) The coefficient of performance is nearly equal to 10
- c) The work done by the motor is nearly 3.36×10^4 J
- d) The power of the momter is nearly 20 kW
- 70. A carnot's engine whose sink is at 27°C has an efficiency of 25%
 - a) The temperature of the source is 400 K
 - b) To increase efficiency by 20%, the temperature of the source should be increased by 28.6°C
 - c) To increase efficiency by 20%, the temperature of the sink should be decreased by 28.6°C
 - d) If the heat energy supplied to the engine is 800 J per cycle the work output per cycle is 200 J
- 71. One mole of oxygen at 27°C is inclosed in a vessel which is thermally insulated. The vessel is moved with a constant speed v and is then suddenly stopped. The process results in a rise of temperature of the gas by 1°C. Then, if M = Molecular mass of oxygen

a)
$$\gamma(=C_p/C_v) = \frac{5}{3}$$
 b) $\gamma = \frac{7}{5}$ c) $v = \sqrt{\frac{R}{M(\gamma+1)}}$ d) $v = \sqrt{\frac{2R}{M(\gamma-1)}}$

72. Figure shows the P - V diagram for an ideal gas. From the graph we conclude that



- a) The process $A \rightarrow B$ is adiabatic
- b) The internal energy of the gas increases in this process
- c) The work done by the gas = area of triangle ABC
- d) The heat energy absorbed by the gas is zero in the process
- 73. The figure shows the *p*-*V* plot of an ideal gas taken through a cycle *ABCDA*. The part *ABC* is a semi-circle and CDA is half of an ellipse. Then,



a) The process during the path $A \to B$ is isothermal b) Heat flows out of the gas during the path $B \to C \to D$

- c) Work done during the path $A \rightarrow B \rightarrow C$ is zero
- d) Positive work is done by the gas in the cycle ABCDA
- 74. Figure shows the P V diagram of a cyclic process. If dQ is the heat energy supplied to the system, dU is the internal energy of the system and dW is the work done by the system, then which of the following relations is/are correct



a) dQ = dUdWb) dU = 0c) dQ = dWd) dQ = -dW75. Figure shows the P - V diagram for an ideal gas. From the graph, we conclude that



a) The process is isothermal

b) The internal energy of the gas remains constant

c) The work done in the process is positive

d) The heat energy absorbed in the process is zero

76. One mole of an ideal gas initial state A undergoes a cyclic process ABCA, as shown in the figure. Its pressure at *A* is p_0 . Choose the correct option (s) from the following.



- a) Internal energies at *A* and *B* are the same
- b) Work done by the gas in process AB is $p_0V_0 \ln 4$

c) Pressure at C is $\frac{p_0}{4}$

d) Temperature at C is $\frac{T_0}{4}$

- 77. Which of the following is incorrect regarding the first law of thermodynamics?
 - a) It is not applicable to any cyclic process
 - b) It is a restatement of the principle of conservation of energy
 - c) It introduces the concept of the internal energy
 - d) It introduces the concept of the entropy
- 78. For an ideal gas
 - The change in internal energy at constant pressure when the temperature of n moles of the gas changes by ΔT is $n C_v \Delta T$

 - b) The change in internal energy of the gas in an adiabatic process is equal in magnitude to the work done by the gas
 - c) The internal energy does not change in an isothermal process
 - d) No heat is added or removed in an adiabatic process
- 79. p V diagram of a cyclic process *ABCA* is shown in figure. Choose the correct statements.



b) $\Delta U_{C \to A}$ =negative c) ΔQ_{CBA} =negative d) $\Delta Q_{B \to} C$ =positive

Assertion - Reasoning Type

This section contain(s) 0 questions numbered 80 to 79. Each question contains STATEMENT 1(Assertion) and STATEMENT 2(Reason). Each question has the 4 choices (a), (b), (c) and (d) out of which **ONLY ONE** is correct.

a) Statement 1 is True, Statement 2 is True; Statement 2 is correct explanation for Statement 1

b) Statement 1 is True, Statement 2 is True; Statement 2 **is not** correct explanation for Statement 1

c) Statement 1 is True, Statement 2 is False

d) Statement 1 is False, Statement 2 is True

80

	Statement 1:	In isothermal process whole of the heat energy supplied to the body is converted into internal energy
	Statement 2:	According to the first law of thermodynamics $\Delta Q = \Delta U + P \Delta V$
81		
	Statement 1:	The entropy of the solids is the highest
	Statement 2:	Atoms of the solids are arranged in orderly manner
82		
	Statement 1:	Efficiency of a Carnot engine increased on reducing the temperature of sink
83	Statement 2:	The efficiency of a Carnot engine is defined as ratio of net mechanical work done per cycle by the gas to the amount of heat energy absorbed per cycle from the source
05	Statement 1.	First law of the numedum emission is no statement of the numerical of concernation of energy
	Statement 1:	First law of thermodynamics is re-statement of the principle of conservation of energy
	Statement 2:	Energy is something fundamental
84		
	Statement 1:	A reversible engine working between 127°C and 227°C cannot have efficiency more than 20%
	Statement 2:	Under ideal conditions $\eta = 1 - \frac{T_2}{T_1}$
85		
	Statement 1:	The heat supplied to a system is always equal to the increase in its internal energy
	Statement 2:	When a system changes from one thermal equilibrium to another, some heat is absorbed by it
86		
	Statement 1:	It is impossible for a ship to use the internal energy of sea water to operate its engine.
	Statement 2:	A heat engine is different from a refrigerator.
87		
	Statement 1:	The Carnot cycle is useful in understanding the performance of heat engines
88	Statement 2:	The Carnot cycle provides a way of determining the maximum possible efficiency achievable with reservoirs of given temperatures

	Statement 1:	If two bodies of equal mass and made of the same material at different temperature T_1 and T_2 are brought in thermal contact, the temperature of each body will be $(T_1 + T_2)/2$ when thermal equilibrium is attained
	Statement 2:	They have the same thermal capacity
89		
	Statement 1:	Specific heat capacity is the cause of formation of land and sea breeze.
	Statement 2:	The specific heat of water is more than land.
90		
	Statement 1:	Change of state is an example of isothermal process
	Statement 2:	Change of state from solid to liquid occurs only at melting point of solid and change of state from liquid to gas occurs only at boiling point of liquid. Thus, there is no change of temperature during change of state
91		
	Statement 1:	Two vessels <i>A</i> and <i>B</i> of equal capacity are connected to each other by a stopcock. Vessel <i>A</i> contains a gas at 0°C and 1 atmosphere pressure and vessel <i>B</i> is evacuated. If the stopcock is suddenly opened, the final pressure in <i>A</i> and <i>B</i> will be 0.5 atmosphere
02	Statement 2:	If the temperature is kept constant, the pressure of a gas is inversely proportional to its volume
92	0	
	Statement 1:	The temperature of the surface of the sun is approximately 6000 K. If we take a big lens and focus the sunrays, we can produce a temperature of 8000 K
	Statement 2:	The highest temperature can be produced according to second law of thermodynamics
93		
	Statement 1:	Work done by a gas in isothermal expansion is more than the work done by the gas in the same expansion, adiabatically
	Statement 2:	Temperature remains constant in isothermal expansion, and not is adiabatic expansion
94		
	Statement 1:	Two vessels <i>A</i> and <i>B</i> are connected to each other by a stopcock. Vessel <i>A</i> contains a gas at 0°C and 1 atmosphere pressure and vessel <i>B</i> is evaluated. The two vessels are thermally insulated from the surroundings. If the stopcock is suddenly opened, there will be no
	Statement 2:	NO transfer of heat energy takes place between the system and the surroundings
95		
	Statement 1:	In an isolated system the entropy increases
	Statement 2:	The processes in an isolated system are adiabatic
96		
	Statement 1:	Heating system based on circulation of steam are more efficient in warming a house than those based or circulation of hot water

Statement 2: The latest heat of steam is high

97

Statement 1: Reversible systems are difficult to find in real world

Statement 2: Most processes are dissipative in nature

98

Statement 1: Efficiency of a Carnot engine decreases with decrease in temperature difference between the source and the sink.

Statement 2:	n - 1	<i>T</i> ₂	$T_1 - T_2$
	η — I =	$\overline{T_1}$	<i>T</i> ₂

99

Statement 1:	In an adiabatic process, change in internal energy of a gas is equal to work done on or by
	the gas in the process
Statement 2:	Temperature of gas remains constant in a adiabatic process

100

Statement 1:	It is not possible for a system, unaided by an external agency to transfer heat from a body
	at a lower temperature to another at a higher temperature
Statement 2:	It is not possible to violate the second law of thermodynamics

101

Statement 1:	Thermodynamic processes in nature are irreversible
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Statement 2: Dissipative effects can not be eliminated

102

Statement 1: A Carnot engine working between 100 K and 400 K has an efficiency of 75%

Statement 2: If follows from $\eta = 1 - \frac{T_2}{T_1}$

103

104

Statement 1:	When a glass of hot milk is placed in a room and allowed to cool, its entropy decreases		
Statement 2:	Allowing hot object to cool does not violate the second law of thermodynamics		

Statement 1: In adiabatic compression, the internal energy and temperature of the system get decreased.Statement 2: The adiabatic compression is a slow process.

105

Statement 1:	When a bottle of cold carbonated drink is opened, a slight fog forms around the opening
Statement 2:	Adiabatic expansion of the gas causes lowering of temperature and condensation of water vapours

Statement 1: Figure shows $\frac{PV}{T}$ versus *P* graph for a certain mass of oxygen gas at two temperatures T_1 and T_2 . It follows from the graph that $T_1 > T_2$



Statement 2: At higher temperatures, real gas behaves more like an ideal gas

107

Statement 1: The isothermal curves intersect each other at a certain point

Statement 2: The isothermal change takes place slowly, so the isothermal curves have very little slope

108

Statement 2: The leaking air undergoes adiabatic expansion

109

	Statement 1:	We can not change the temperature of a body without giving (or taking) heat to (or from) it
	Statement 2:	According to principle of conservation of energy, total energy of a system should remain conserved
110		
	Statement 1:	The isothermal curves intersect each other at a certain point
	Statement 2:	The isothermal changes takes place rapidly, so the isothermal curves have very little slope
111		
	Statement 1:	Internal energy of an ideal gas depends only on temperature and not on volume
	Statement 2:	Temperature is more important than volume
112		
	Statement 1:	If an electric fan be switched on in a closed room, the air of the room will be cooled
	Statement 2:	Fan air decreases the temperature of the room
113		
	Statement 1:	Zeroth law of thermodynamic explains the concept of energy
	Statement 2:	Energy is dependent on temperature
114		

Statement 1: An adiabatic process is an isotropic process

115		
	Statement 1:	First law of thermodynamic does not forbid flow of heat from lower temperature to higher temperature.
	Statement 2:	Heat supplied to a system is always equal to the increase in its internal energy at constant volume.
116		
	Statement 1:	Two vessels <i>A</i> and <i>B</i> are connected to each other by a stopcock. Vessel <i>A</i> contains a gas at 300 K and 1 atmosphere pressure and vessel <i>B</i> is evacuated. The two vessel are thermally insulated from the surroundings. If the stopcock is suddenly opened, the
	Statement 2:	expanding gas does no work Since $\Delta Q = 0$ and $\Delta U = 0$, it follows from the first law of thermodynamics thet $\Delta W = 0$
117		
	Statement 1:	The specific heat of a gas in an adiabatic process is zero and in an isothermal process is infinite
	Statement 2:	Specific heat of a gas is directly proportional to change of heat in system and inversely proportional to change in temperature
118		
	Statement 1:	It is not possible for a system, unaided by an external agency to transfer heat from a body at lower temperature to another body at higher temperature
	Statement 2:	According to Clausius statement, "No process is possible whose sole result is the transfer of heat from a cooled object to a hotter object

Statement 2: $\Delta S = \frac{\Delta Q}{T} = 0 \therefore \Delta Q = 0$, Which represents an adiabatic process

Matrix-Match Type

This section contain(s) 0 question(s). Each question contains Statements given in 2 columns which have to be matched. Statements (A, B, C, D) in **columns I** have to be matched with Statements (p, q, r, s) in **columns II**.

119. Column I contains a list of processes involving expansion of an ideal gas. Match this with Column II describing the thermodynamic change during this process

Column- II

(p) The temperature of the gas decreases

(A) An insulated container has two chambers separated by a valve. Chamber I contains an ideal gas and the Chamber II has vacuum. The valve is opened

Column-I



- **(B)** An ideal monoatomic gas expands to twice its original volume such that its pressure $P \propto \frac{1}{V^2}$, where *V* is the volume of the gas
- (C) An ideal monoatomic gas expands to twice its original volume such that its pressure $P \propto \frac{1}{V^{4/3}}$, where *V*, is its volume
- (q) The temperature of the gas increases or remains constant
- (r) The gas loses heat

(D) An ideal monoatomic gas expands such that its (s) The gas gains heat pressure *P* and volume *V* follows the behavior shown in the graph

Р

CODES:

	Α	В	С	D
a)	P,r	q	q,s	p,s
b)	q	p,r	p,s	q,s
c)	p,s	q,s	q	p,r
d)	q,s	p,s	p,r	q

120. Match the following for the given process



Column- II

(q) W < 0(r) W > 0

(p) Q > 0

(s) Q < 0

	Α	В	С	D
a)	S	p,r	r	q,s
b)	p,r	q,s	S	r
c)	q,s	S	p,r	r
d)	S	r	q,s	p,r

121. One mole of a monoatomic ideal gas is taken through a cycle *ABCDA* as shown in the *P*-*V* diagram. Column-II given the characteristics involved in the cycle. Match them with each of the processes given in Column-I



	Α	В	С	D
a)	P,r	q,s	r,t	p,r,t
b)	r,t	p,r,t	p,r	q,s
c)	p,r,t	p,r	q,s	r,t
d)	q,s	r,t	p,r,t	p,r

Column- II

- (p) Internal energy decreases
- (q) Internal energy increases
- (r) Heat is lost
- (s) Heat is gained
- (t) Work is done on the gas

Linked Comprehension Type

This section contain(s) 16 paragraph(s) and based upon each paragraph, multiple choice questions have to be answered. Each question has atleast 4 choices (a), (b), (c) and (d) out of which **ONLY ONE** is correct. **Paragraph for Question Nos. 122 to -122**

The efficiency of a Carnot engine working between source temperature T_1 and sink temperature T_2 is $\eta = 1 - \frac{T_2}{T_1}$. The efficiency cannot be 100% as we cannot maintain $T_2 = 0$. Coefficient of performance of a refrigerator

working between the same two temperature is

Coefficient of performance $\frac{T_2}{T_1 - T_2} = \frac{1 - \eta}{\eta}$

122. The efficiency of a Carnot engine working between 27°C and -73°C isa) 100%b) 60%c) 33%d) Zero

Paragraph for Question Nos. 123 to - 123

The changes in pressure and volume of a gas when heat content of the gas remains constant are called adiabatic changes. The equation of such changes is pV^{γ} = constant. The changes must be sudden and the container must be perfectly insulting to disallow any exchange of heat with the surrounding. In such changes, dQ = 0. As per first law of thermodynamics, dQ = dU + W = 0. Therefore, dU = -dW.

123. A gas in a container is compressed suddenly. Its temperature would

- a) Increase
- b) Decrease
- c) Stay constant
- d) Change depending upon surrounding temperature.

Paragraph for Question Nos. 124 to - 124

Three moles of an ideal gas $\left(C_p = \frac{7R}{2}\right)$ at pressure P_A and temperature T_A are isothermally expanded to twice the original volume. The gas is then compressed at constant pressure to its original volume. Finally the gas is heated at constant volume to its original pressure P_A

124. Which of the graphs shown in Fig. represents the P - V diagram for the complete process?



Paragraph for Question Nos. 125 to - 125

Two moles of an ideal gas at volume *V*, pressure 2 *P* and temperature *T* undergo a cyclic process *ABCDA* as shown in Fig.





a) $\frac{V}{2}$	b) $\frac{2V}{2}$	c) <i>V</i>	d) $\frac{4V}{2}$
3	3		3

Paragraph for Question Nos. 126 to - 126

Two moles of a monoatomic ideal gas occupy a volume *V* at 27°C. The gas is expanded adiabatically to volume $2\sqrt{2} V$. Gas constant $R = 8.3 \text{ JK}^{-1} \text{mol}^{-1}$

126. The final temperature of the gas is a) $\frac{150}{\sqrt{2}}$ K b) 150 K c) $150\sqrt{2}$ K d) 13.6°C

Paragraph for Question Nos. 127 to - 127

A sample of 2 kg of monoatomic helium (assumed ideal) is taken through the process *ABC* and another sample of 2 kg of the same gas is taken through the process *ADC* as shown in Fig. The molecular mass = 4 and $R = 8.3 \text{ J K}^{-1} \text{mol}^{-1}$



127. The temperature	of state A is		
a) 100 K	b) 200 K	c) 300 K	d) 415 K

Paragraph for Question Nos. 128 to - 128

One mole of an ideal monoatomic gas is taken round the cyclic process ABCA as shown in Fig.



128. The work done b	y the gas is		
a) $P_0 V_0$	b) $2P_0V_0$	c) $3P_0V_0$	d) $4P_0V_0$

Paragraph for Question Nos. 129 to - 129

Two moles of an ideal monoatomic gas, initially at pressure $P_1 = P$ and volume $V_1 = 2\sqrt{2} V$, undergo an adiabatic compression until its volume is $V_2 = V$ and the pressure is P_2 . Then the gas is given heat energy Q at constant volume V_2

129. Which of the graphs shown in Fig. represents the P - V diagram of the complete process?



Paragraph for Question Nos. 130 to - 130

Two moles of an ideal mono-atomic gas is taken through a cycle *ABCA* as shown in the P - T diagram (Fig). During the process *AB*, pressure and temperature of the gas vary such that PT = K, where *K* is a constant



130. Constant *K* is given by a) $\frac{P_1T_1}{2}$ b) P_1T_1 c) $2P_1T_1$

Paragraph for Question Nos. 131 to - 131

A monoatomic ideal gas of 2 moles is taken through a cyclic process starting from A as shown in Fig



d) $\sqrt{2}P_1T_1$

Given $\frac{V_B}{V_A} = 2$ and $\frac{V_D}{V_A}$ 4. The temperature $T_A = 27^{\circ}$ C. *R* is the gas constant

131. The temperature	e of the gas at point <i>B</i> is		
a) 400 K	b) 500 K	c) 600 K	d) 700 K

Paragraph for Question Nos. 132 to - 132

Two moles of helium gas are taken over the cycle *ABCDA*, as shown in the P - T diagram



132. Assuming the gas to be ideal the work done on the gas in taking it from A to B isa) 200 Rb) 300 Rc) 400 Rd) 500 R

Paragraph for Question Nos. 133 to - 133

A small spherical monoatomic ideal gas bubble $\left(\gamma = \frac{5}{3}\right)$ is trapped inside a liquid of density ρ_1 (see figure). Assume that the bubble does not exchange any heat with the liquid. The bubble contains *n* moles of gas. The temperature of the gas when the bubble is at the bottom is T_0 , the height of the liquid is *H* and the atmospheric pressure is P_0 (Neglect surface tension)



133. As the bubble moves upwards, besides the buoyancy force the following forces are acting on it

- a) Only the force of gravity
- b) The force due to gravity and the force due to the pressure of the liquid
- c) The force due to gravity, the force due to the pressure of the liquid and the force due to viscosity of the liquid
- d) The force due to gravity and the force due to viscosity of the liquid

12.THERMODYNAMICS

						ANS	W
1)	h	2)	C	3)	d	4)	h
-) 5)	d	-) 6)	a	3) 7)	u h	+) 8)	d b
9) 9)	u h	0) 10)	d d	7) 11)	C	0) 12)	u a
2) 13)	d	14)	u a	15)	с а	16)	a h
13J 17)	u a	17) 10)	a h	10)	a	20)	U C
1/J 21)	a	10J 22)	U	19J	U h	20J 24)	ט ג
21J 25)	a J	22)	C J	235	D	24J 20)	u J
25)	a	26)	a	27)	а	28)	a
29)	C	30)	b	31)	а	32)	d
33)	d	34)	а	35)	С	36)	a
37)	С	38)	а	39)	а	40)	b
41)	d	42)	b	43)	d	44)	d
45)	С	46)	b	47)	d	48)	b
49)	b	50)	а	51)	b	52)	d
53)	С	54)	С	1)	a,b,c	2)	
	a,c	3)	a,b,c,d	4)	a,c,d		
5)	a,b,c	6)	d	7)	a,c	8)	
-	a,b	-		-	-	-	
9)	a,b.c	10)	a,b.c.d	11)	b,c	12)	
,	a,b.c.d	1	, - , - , -	,		,	
13)	a.h.d	14)	b.c	15)	a.b.c.d	16)	
,	a.h.d	- •)	~,•	,		,	
17)	h d	18)	h	19)	h d	20)	ſ
	ahc	-0j 221	ah	- 7J 221	a d	20) 24)	Ľ
	ahcd	,	ajb	23)	uju	- 1)	
25)	a, b, c, d	' 1)	d	2)	Ь	3)	h
235	a,c,u 4)	I) C	u	23	u	3)	U
5)	4J	C C	d	7)	h	0)	-
5J	a	0J	a	/]	D	ØJ	а
9J	a	10)	a	11)	а	12)	a
13)	d	14)	b	15)	а	16)	b
17)	а	18)	а	19)	а	20)	С
21)	а	22)	а	23)	а	24)	b
25)	d	26)	а	27)	а	28)	d
29)	а	30)	d	31)	d	32)	С
33)	d	34)	d	35)	а	36)	b
37)	а	38)	а	39)	а	1)	b
	2)	а	3)	С	1)	С	
	2)	а	3)	с	4)	d	
5)	b	6)	a	7)	a	8)	с
9)	с	10)	с	11)	С	12)	d
,		,		,		,	

: HINTS AND SOLUTIONS :

6

1 **(b)**

dQ = dU + dW In an adiabatic process, dQ = 0Hence dU = -dW = -4.5 J

2 **(c)**

The two adiabatic paths *ad* and *bc* for the gas intersect the two isothermals *ab* and *cd* at temperatures T_1 and T_2 (see Fig.). Since points *a* and *d* lie on the same adiabatic path, we have $T V^{(\gamma-1)} - T V^{(\gamma-1)}$

$$\operatorname{Or}\left(\frac{V_a}{V_d}\right)^{(\gamma-1)} = \frac{T_2}{T_1} \qquad (1)$$

Since points *b* and *c* also lie on the same adiabatic path,

$$T_{1}(V_{b})^{(\gamma-1)} = T_{2} V_{c}^{(\gamma-1)}$$

Or $\left(\frac{V_{b}}{V_{c}}\right)^{(\gamma-1)} = \frac{T_{2}}{T_{1}}$ (2)
From (1) and (2), we get
 $\left(\frac{V_{a}}{V_{d}}\right)^{(\gamma-1)} = \left(\frac{V_{b}}{V_{c}}\right)^{(\gamma-1)}$
Or $\frac{V_{a}}{V_{d}} = \frac{V_{b}}{V_{c}}$

Given $C_p - C_v = 4150$ and $C_p/C_v = 1.4$ or $C_p = 1.4 C_v$. Therefore, $1.4 C_v - C_v = 4150$ Or $C_v = \frac{4150}{0.4} = 10375$ J kg⁻¹K⁻¹

4 **(b)**

In process *AB*, the volume *V* increases linearly with temperature *T*. Hence process *AB* is isobaric (constant pressure). Therefore, work done in this process is

$$W_{AB} = P\Delta V = nR\Delta T (\because PV = nRT)$$

= $nR(T_B - T_A)$
= $3 \times 8.3 \times (200 - 100) = 2490 \text{ J}$
Process *CA* is isochoric (constant volume). Hence
work done in this process $W_{CA} = 0$. Since the
whole process *ABCA* is cyclic, the change in
internal energy in the complete cycle is zero, i.e.
 $\Delta U = 0$. Now, from the first law of
thermodynamics, (Given $Q = -2510$ J)
 $Q = \Delta U + W = \Delta U + W_{AB} + W_{BC} + W_{CA}$
Or $-2510 = 0 + 2490 + W_{BC} + 0$
Or $W_{BC} = -2510 - 2490 = -5000 \text{ J}$
The negative sign shows that the work is done by
the gas

Heat produced is given by $dQ = \frac{V^2 t}{R} = \frac{(10)^2 \times (10 \times 60)}{50} = 1200 \text{ J}$ Since the container is rigid, the change in volume dV = 0. Hence work done dQ = PdV = 0. Fromthe first law of thermodynamics, the change in internal energy is dU = dQ - dW = dQ = 1200 J(a) $T_2 = 300 \text{ K} \cdot \text{Now } \eta = 1 - T_2/T_1. \text{ When}$ $\eta = 40\% = 0.4$, the value of T_1 is given by $\frac{T_2}{T_1} = 1 - 0.4 = 0.6$ Or $T_1 = \frac{T_2}{0.6} = \frac{300}{0.6} 500 \text{ K}. \text{When} \eta = 60\%, =0.6$, the value of T_2 should be $T_2' = \frac{300}{0.4} = 750 \text{ K}$ $\therefore T_2' - T_2 = 750 - 500 = 250 \text{ K}$

7 **(b)**

The speed of sound in gas of bulk modulus *B* and density ρ is given by

$$v = \sqrt{\frac{B}{\rho}}$$

Bulk modulus *B* is given by $B = -\frac{V\Delta P}{\Delta V}$

Now, for a perfect gas, PV = nRT. Differentiating at constant *T*, we get

$$P\Delta V + V\Delta P = 0 \text{ or } \frac{V\Delta P}{\Delta V} = -P$$

Hence
$$v = \sqrt{\frac{P}{\rho}}$$

If m is the mass of the gas and M its molecular mass, then

$$PV = \frac{m}{M} RT \text{ or } PM = \frac{mRT}{V} = \rho RT$$

$$Or \frac{P}{\rho} = \frac{RT}{M} \text{ or } v^2 = \frac{RT}{M}$$

$$Or v = \sqrt{\frac{RT}{M}}$$

Hence $v_1 = \sqrt{\frac{RT}{M_1}}$ and $v_2 = \sqrt{\frac{RT}{M_2}}$ which

$$Give \frac{v_1}{v_2} = \sqrt{\frac{M_2}{M_1}}$$

(d)

8

Since the temperature T remain constant along the path CA, P will be inversely proportional to Valong this path. Hence, as P increases, V must decrease in a nonlinear fashion. This is represented by the curve CA in Fig. Along the path BC, the volume V is constant. Hence the graph of *P* against *V* is a straight line perpendicular to the *V*-axis. On a P - V diagram, the corresponding path is *BC* as shown in Fig. For the path *AB*, *V* is directly proportional to *T* pressure remaining constant. The corresponding path *AB* is, therefore a straight line parallel to the *V*-axis. Thus the cyclic process on a P - V diagram is represented by choice (d) in Fig.



9 (b)

Since the P - V graph is a straight line with a positive slope, $P \propto V$

 $\operatorname{Or} PV^{-1} = \operatorname{constant}$

For a process in which $PV^n = \text{constant}$, the molar heat capacity is given by

$$C = \frac{R}{(\gamma - 1)} + \frac{R}{1 - r}$$

Putting n = -1 and $\gamma = \frac{5}{3}$ (for a monoatomic gas), we have

$$C = \frac{R}{\left(\frac{5}{3} - 1\right)} + \frac{R}{(1+1)} = \frac{3R}{2} + \frac{R}{2} = 2R$$

10 (d)

Work done on the gas is $\Delta W = P\Delta V = P(V_f - V_i)$ $= 1 \times 10^5 \times (25 - 5) \times 10^{-3}$ = 2000 J

The internal energy is given by $U = \frac{PV}{(\gamma-1)}$

$$\therefore U_i = \frac{PV_i}{(\gamma - 1)}, U_f = \frac{PV_f}{(\gamma - 1)}$$

Therefore, change in internal energy is

$$\Delta U = U_f - U_i = \frac{P}{(\gamma - 1)}(V_f - V_i)$$
$$= \frac{1 \times 10^5 \times (25 - 5) \times 10^{-3}}{(1.4 - 1)} = 5000 \text{ J}$$

From the first law of thermodynamics, the heat energy supplied to the gas is $\Delta Q = \Delta W + \Delta U = 2000 + 5000$ = 7000 J

11 **(c)**

 $p^{V^{\gamma}} = \text{constant. For a given mass of gas, } V \propto \frac{1}{d}$ Hence $\frac{p}{d^{\gamma}} = \text{constant}$ $\therefore \frac{p_1}{d_1^{\gamma}} = \frac{p_2}{d_2^{\gamma}}$

Or
$$\frac{p_2}{p_1} = \left(\frac{d_2}{d_1}\right)^{\gamma} = (32)^{7/5} = (2)^7 = 128$$

(a)

For a monoatomic gas, $C_v = 3R/2$ and for a diatomic gas, $C_v = 5R/2$. Since one mole of each gas is mixed together, the C_v of the mixture will

$$C_{v} = \frac{1}{2} \left[\frac{3R}{2} + \frac{5R}{2} \right] = 2R$$

Now $C_p - C_v = R$. Therefore, for the mixture, $C_p = R + C_v = R + 2R = 3R$. Hence, the ratio of the specific heats of the mixture is

$$\gamma = \frac{C_p}{C_v} = \frac{3R}{2R} = \frac{3}{2} = 1.5$$

13 **(d)**

12

Oxygen is diatomic gas, hence its energy of two moles

$$= 2 \times \frac{5}{2}RT = 5RT$$

Argon is a monoatomic gas, hence its internal energy of 4 moles = $4 \times \frac{3}{2}RT = 6RT$ Total Internal energy = (6 + 5)RT = 11RT

14 **(a)**

In the process $A \rightarrow B$, V is proportional to T. Hence pressure P remains constant. Therefore, heat energy absorbed in this process is (:: $C_p = 7 R/2$ for a diatomic gas)

$$(Q)_{A \to B} = n C_p \Delta T = n \times \frac{7R}{2} \times (2T_0 - T_0)$$
$$= \frac{7}{2} n RT_0$$

Process $B \rightarrow C$ is isothermal in which the gas is compressed. Hence, work done on the gas in this process is

$$(W)_{B \to C} = -nR(2T_0) \ln\left(\frac{V_0}{2V_0}\right)$$

= $-2 n RT_0 \ln\left(\frac{1}{2}\right)$
= $2 n RT_0 \ln(2)$
 $\therefore \frac{(Q)_{A \to B}}{(W)_{B \to C}} = \frac{7}{4 \ln(2)}$, Which is choice (a)

16 **(b)**

Given $T_1 = 0^{\circ}\text{C} = 273 \text{ K}, T_2 = 400^{\circ}\text{C} = 673 \text{ K}$ Work done $W = \frac{nR}{(\gamma - 1)} (T_2 - T_1) = \frac{5 \times 8.3 \times 400}{\left(\frac{7}{5} - 1\right)}$

By convention, the work done on the gas is taken to be negative, i.e. W = -41.5 kJ From the first law of thermodynamics dQ = dU + dW For an adiabatic process, dQ = 0 Hence dU = -dW =-(-41.5) = 41.5 kJ The positive sign of dUimplies that the internal energy increases

17 (a)

22.4 L of any gas is 1 mol,

$$\therefore \quad 5.6 \text{ L} = \frac{5.6}{22.4} = \frac{1}{4} \text{ mol} = n$$

In adiabatic process,

$$TV^{\gamma-1} = \text{constant}$$

$$\therefore \quad T_2 V_2^{\gamma-1} = T_1 V_1^{\gamma-1}$$

or

$$T_2 = T_1 \left(\frac{V_1}{V_2}\right)^{\gamma-1}$$

 $\gamma = \frac{C_P}{C_V} = \frac{5}{3}$ for monoatomic He gas

$$\therefore \quad T_2 = T_1 \, \left(\frac{5.6}{0.7}\right)^{\frac{5}{3}-1} = 4T_1$$

Further in adiabatic process,

0 = 0

$$\therefore W + \Delta U = 0$$

or
$$W = -\Delta U = -nC_V \Delta T$$

$$= -n \left(\frac{R}{\gamma - 1}\right) (T_2 - T_1)$$
$$= -\frac{1}{4} \left(\frac{R}{\frac{5}{3} - 1}\right) (4T_1 - T_1)$$
$$= -\frac{9}{8} RT_1$$

18 **(b)**

For an adiabatic process, $PV^{\gamma} = \text{constant}$, Differentiating, we have $\gamma P V^{\gamma - 1} + \frac{dP}{dV} V^{\gamma} = 0 \text{ or } \frac{dP}{dV} = -\frac{\gamma P}{V}$ Since at any instant $PV = \text{constant}, \frac{dP}{dV} \propto \gamma$, i.e. the slope of P - V curve is proportional to γ . Now, for a diatomic gas, γ (= 7/5) is than that of for a monoatomic gas for which $\gamma = 5/3$. Therefore, the slope of the P - V curve is less for a diatomic gas than for a monoatomic gas. Hence curve 1 corresponds to diatomic gas and curve 2 to monoatomic gas

19 (c)

$$PV^{2/3} = k \qquad ($$

1) Equation of state is $PV = n R T \Rightarrow P = \frac{n R T}{v}$ Using this in Eq. (1) we get

$$\frac{n R T}{V} \times V^{2/3} = k$$

Or $TV^{-1/3} = \frac{k}{n R} = \text{constant}$
Hence $V \propto T^3$

20 (c)

Heat energy supplied $dQ = C_p dT$. Change in internal energy $dU = C_{\nu} dT$. Therefore, work done $dW = dQ - dU = (C_p - C_v)dT$

$$\therefore \frac{dW}{dQ} = \frac{(C_p - C_v)dT}{C_p dT} = 1 - \frac{1}{\gamma}$$
$$= 1 - \frac{1}{5/3} = \frac{2}{5}$$

(:: $\gamma = 5/3$ for a monoatomic gas)

21 (a)

Process *AB* is isochoric, i.e. the volume remains constant. Thus $\Delta V = 0$. Hence work done $P\Delta V =$ 0. Process *BC* is isobaric, i.e. the pressure remains constant and external work has to be done. The work done = $P_B \times (V_D - V_A) = 8 \times 10^4 \times$ $(5 \times 10^{-3} - 2 \times 10^{-3}) = 240$ J. Therefore, change in internal energy is

dU = dQ - dW = 800 - 240 = 560 J

For a gas,
$$PV = nRT$$
 Hence
(1 mole) PT

$$(P)_{02} = \frac{(1 \text{ mole}) R1}{V}$$
And
$$(P)_{\text{He}} = \frac{(1 \text{ mole}) R(2T)}{V}$$

$$\therefore \frac{(P)_{\text{He}}}{(P)_{0_2}} = 2$$
Or $(P)_{\text{He}} = 2(P)_{02}$

23 **(b)**

The internal energy of *n* moles of an ideal gas at temperature T is given by

$$U = \frac{f}{2} n R T$$

Where f = number of degrees of freedom For hydrogen, f = 5. Therefore $U_1 = \frac{5}{2} \times 3 \times RT = \frac{15}{2} RT$

For helium,
$$f = 3$$
. Therefor
 $U_2 = \frac{3}{2} n R (T/2) = \frac{3}{4} n RT$
Given $U_1 = U_2$, i.e.
 $\frac{15}{2} RT = \frac{3}{4} n R T$
Which gives $n = 10$

24 (d)

> In the process $B \rightarrow A$, work is done on the gas. Hence $(\Delta W)_{B\to A} = -50$ J. Since this process is

adiabatic, $(\Delta Q)_{B \to A} = 0$. From the first law of thermodynamics, the change in internal energy in this process is $(\Delta U)_{B \to A} = (\Delta Q)_{B \to A} - (\Delta W)_{B \to A}$ = 0 - (-50) = +50 JSince the process is cyclic, there is no net change in internal energy. Hence $(\Delta U)_{A \to B} =$ $-(\Delta U)_{B \to A} = -50 \text{ J}$ (d) For an adiabatic process

25 **(d)**

For an adiabatic process $TP^n = k$ Where $n = \frac{(1-\gamma)}{\gamma}$, $\gamma = \frac{C_p}{C_v}$ and k is a constant Therefore, $p = {\binom{k}{1}}^{1/n}$

$$P = \left(\frac{\pi}{T}\right)$$

Since n = constant for a given gas, $P \propto T^{-1/n}$

Given $P \propto T^3$ Hence $-\frac{1}{n} = 3$ or $-\frac{\gamma}{1-\gamma} = 3$, Which Gives $\gamma = \frac{3}{2}$

26 **(d)**

For adiabatic process, $T_1 V_1^{(\gamma-1)} = T_2 V_2^{(\gamma-1)}$ Thus, $\frac{T_1}{T_2} = \left(\frac{V_2}{V_1}\right)^{(\gamma-1)}$ For a monoatomic gas, $\gamma = 5/3$. Also $V_2/V_1 = L_2/L_1$ Hence $\frac{T_1}{T_2} = \left(\frac{L_2}{L_1}\right)^{\left(\frac{5}{3}-1\right)} = \left(\frac{L_2}{L_1}\right)^{2/3}$

From the first law of thermodynamics, we have dU = dQ - dW

Given dW = 0 and dQ < 0. Hence the change in internal energy dU < 0. Now, for an ideal gas, the internal energy can decrease only by decrease in temperature

28 (d)

Heat is given to the gas in cylinder *A* at constant pressure while the same amount of heat is given to the gas in cylinder *B* at constant volume. Heat given to gas in *A* is

$$Q_A = n C_p \Delta T_p$$

Heat given to gas in *B* is $Q_B = n C_v \Delta T_B$ Since $Q_A = Q_B$, we have $nC_p \Delta T_A = nC_v \Delta T_B$ Or $\Delta T_B = \frac{C_p}{C_v} \Delta T_A = \frac{7}{5} \times 30 \text{ K} = 42 \text{ K}$ (::for a diatomic gas, $C_p/C_v = 7/5$)

The equation of state for an ideal gas of mass m

and molecular mass *M* is $PV = \frac{m}{M} RT$ (i) For an isothermal process, *T* = constant. Differentiating (i) partially at constant *T*, we get $P\Delta V + V\Delta P = 0$ Or $\Delta P = -P \frac{\Delta V}{V}$ (ii) From (i), $P = \frac{mRT}{MV}$. Using this in (ii), we get $\Delta P = -\frac{mRT}{MV}$ ($\because \Delta V = 2V - V = V$) $\therefore \Delta P_A = -\frac{m_A RT}{MV}$ and $\Delta P_B = -\frac{m_B RT}{MV}$ Hence $\frac{\Delta P_A}{\Delta P_B} = \frac{m_A}{m_B}$ Given $\Delta P_B = 1.5 \Delta P_A$. Therefore, $\frac{1}{1.5} = \frac{m_A}{m_B}$ Or $3 m_A = 2 m_B$ 30 **(b)** Number of moles in 8 g of oxygen(*n*) = $\frac{1}{4}$. Now the

equation of state for *n* moles of an ideal gas is $PV = n R T = \frac{1}{4} \times RT = \frac{RT}{4}$

31 **(a)**

Since the slope of the P - V graph for adiabatic expansion is γ times that for isothermal expansion, curves *AB* and *AC* in Fig. respectively represent isothermal and adiabatic expansions of the gas from initial volume V_1 to final volume V_2



AS the area under curve *AB* between volumes V_1 and V_2 is greater than the area under curve *AC* between V_1 and V_2 , it follows that $W_1 > W_3$ Figure (b) shows the P - V graph for isobaric (at constant pressure) expansion from initial volume V_1 and pressure P_1 to final volume V_2 ; the pressure remaining unchanged at P_1 . Comparing figures (a) and (b) we find that the area under *AD* between volumes V_1 and V_2 is greater than the area under curves *AB* and *AC*. Hence W_2 is greater than W_1 and W_3

$$\Delta Q = nC_P \Delta T$$
$$= 2\left(\frac{3}{2}R + R\right) \Delta T$$
$$= 2\left[\frac{3}{2}R + R\right] \times 5$$

$$= 2 \times \frac{5}{2} \times 8.31 \times 5$$
$$= 208 J$$

33 **(d)**

Let *L* be the length (in cm) of the hollow cylinder and *r* its radius. Since the mass of the gas remains unchanged and the pressures of the gas in both sides are equal, we have, from Charle's law,

$$\frac{v_1}{T_1} = \frac{v_2}{T_2}$$
(1)
Given $V_1 = \left(\frac{L}{2} - 5\right) \pi r^2$, $V_2 = \left(\frac{L}{2} + 5\right) \pi r^2$,
 $T_1 = 0^{\circ}\text{C} = 273 \text{ Kand } T_2 = 100^{\circ}\text{C} = 373 \text{ K. Using these values in (1), we get}$

$$\frac{\frac{L}{2} - 5}{273} = \frac{\frac{L}{2} + 5}{373}$$

Which gives $L = 64.6$ cm

$$E_{\theta} =$$

Р

35 **(c)**

Let ΔT be the increase in temperature when the volume of the gas is changed by ΔV at constant pressure. The change in internal energy of n moles of a gas is given by

$$\Delta U = n C_v \Delta T \quad (i)$$

We know that $C_p - C_v = R$
Or $\frac{C_p}{C_v} = 1 + \frac{R}{C_v}$. But $\frac{C_p}{C_v} = \gamma$
Therefore, $\gamma = 1 + \frac{R}{C_v}$, which gives

$$C_v = \frac{R}{(\gamma - 1)} \quad \text{(ii)}$$

Also PV = n RT. At constant pressure, when volume changes by ΔV , the change in temperature ΔT is given by

 $P\Delta V = n R\Delta T$ $Or \Delta T = \frac{P\Delta V}{nR} = \frac{PV}{nR}$ $(\because \Delta V = 2V - V = V) \quad (iii)$ Using (ii) and (iii) in (i) we have $\Delta U = n \times \frac{R}{m} \times \frac{PV}{m} = \frac{PV}{m}$

$$U = n \times \frac{1}{(\gamma - 1)} \times \frac{1}{nR} = \frac{1}{(\gamma - 1)}$$

36 **(a)**

Expanding the equation of state we have $PV^{c} + aT^{2}V^{c-1} = RT + b$ Or $P = -aT^{2}V^{-1} + RTV^{-c} + bV^{-c}$ Or $P = AV^{-c} - BV^{-1}$ (i) Where A = RT + b and $B = aT^{2}$. We are given that $P = AV^{m} - BV^{n}$ (ii) Comparing the powers of V in (i) and (ii) we get m = -c and n = -1 Heat energy absorbed = work done = area of the loop

$$=\pi r^2 = \pi d^2/4 = \frac{\pi}{4}(30-10)^2 = 10^2 \pi$$
 joule

38 **(a)**

Let T_0 be the temperature of the mixture. Since the total internal energy remains unchanged, we have

 $\begin{array}{l} U \text{ of mixture} = U_1 + U_2 \\ \Rightarrow (n_1 + n_2) C_v T_0 = n_1 C_v T_1 + n_2 C_v T_2 \\ \Rightarrow (n_1 + n_2) T_0 = n_1 T_1 + n_2 T_2 \\ \Rightarrow (2 + 3) T_0 = 2T + 3 \times (2T) = 8T \\ \text{Which gives } T_0 = \frac{8T}{5} \end{array}$

39 **(a)**

For an ideal gas, PV = nRT. Since pressure *P* is kept constant,

$$P\Delta V = n R\Delta T$$

Or $\frac{\Delta V}{\Delta T} = \frac{nR}{P} = \frac{n RV}{nRT} = \frac{V}{T} \left(\because P = \frac{n RT}{V} \right)$
Or $\frac{1}{V} \frac{\Delta V}{\Delta T} = \frac{1}{T}$ or $\delta = \frac{1}{T}$

Thus, the value of δ decreases as *T* is increased Hence the correct choice is (c)

40 **(b)**

Given
$$V = \frac{kT^n}{P}$$
. Since $P = \text{constant}$,
 $dV = \frac{kn}{P}T^{(n-1)} dT$
Work done $W = \int P \, dV = kn \int T^{(n-1)} \, dT$
 $= kT^n + c$
Where $c = \text{constant of integration}$

41 **(d)**

Heat energy required to raise the temperature of *n* moles of a gas by ΔT at constant pressure is $Q_p = n C_p \Delta t$

Heat energy required to raise the temperature n moles of a gas by ΔT at constant volume is

$$Q_{\nu} = n C_{\nu} \Delta T, \therefore \frac{Q_{\nu}}{Q_{p}} = \frac{C_{\nu}}{C_{p}}$$

Or $Q_{\nu} = \frac{C_{\nu}}{C_{p}} \times Q_{p} = \frac{3 R/2}{3 R/2} \times Q_{p}$
 $= \frac{3}{5} \times 207 = 124.2 = 124 J$

42 **(b)**

For monoatomic gas,

$$C_P = \frac{5}{2}R$$

And $C_V = \frac{3}{2}R$

For diatomic gas,

$$C_P = \frac{7}{2}R$$

 $C_V = \frac{5}{2}R$ and

43 (d)

Since the volume of the gas is constant,

$$\frac{P_1}{P_2} = \frac{T_1}{T_2} \quad (1)$$
Now $P_2 = P_1 + 0.02 \quad P_1 = 1.02 \quad P_1 \text{ and } T_2 = T_1 + 0.02 \text{ J}_1 \text{ sing these values in Eq. (1), we have$

$$\frac{P_1}{1.02 P_1} = \frac{P_1}{T_1 + 5} \Rightarrow T_1 = 250 \text{ K}$$

 $PV = \frac{m}{M} RT$. Therefore, the density of the gas is $\rho = \frac{m}{V} = \frac{P M}{RT} = \frac{PmN}{RT} = \frac{mP}{kT}$

45 (c)

Volume \propto (diameter)³. Since the diameter of the bubble is doubled in rising from the bottom to the top of the lake, its volume becomes 8 times. Now PV = constant. Therefore, the pressure at the bottom of lake = 8 times that at the top. Let H be the depth of the lake

$$H \rho_w g = (8h - h)\rho_m g$$

Or $H = 7h \frac{\rho_m}{\rho_w} = 7 h\rho \left(\because \rho = \frac{\rho_m}{\rho_w} \right)$

46 **(b)**

 $\Delta U = C_v \Delta T$. Now $C_p - C_v = R$ or $\frac{C_p}{C_v} - 1 = \frac{R}{C_v}$ Or $C_{\nu} = \frac{R}{\gamma - 1}$, where $\gamma = \frac{C_p}{C_{\nu}}$. Hence $\Delta U = \frac{R\Delta T}{(\gamma - 1)} = \frac{8.3 \times 8}{(1.4 - 1)} = 166 \text{ J}$

47 (d)

When work is converted into heat at a constant temperature, the entropy of the system remains constant

48 (b)

Now $Q_p = n C_p \Delta T$ and $Q_v = n C_v \Delta T$. But Q_v gives the heat energy which increases the internal energy of the gas. Thus the required fraction is $\frac{Q_{\nu}}{Q_{p}} = \frac{C_{\nu}}{C_{p}} = \frac{1}{\gamma} = \frac{1}{5/3} = \frac{3}{5}$

 $\left(\because \text{ for monoatomic gas } \gamma = \frac{5}{2}\right)$

Work done = area enclosed by the indicator diagram ABC

$$= \frac{1}{2} \times BC \times AC$$
$$= \frac{1}{2} \times (4P - P) \times (3V - V)$$
$$= 3 PV$$

50 (a)

5

Given $T = kV^2$. Therefore dT = 2 kV dV or dT

$$aV = \frac{1}{2kV}$$
Also $PV = n R T \Rightarrow P = \frac{n R T}{V}$

$$\therefore \text{ Work done } w = \int_{T}^{3T} P dV$$

$$= \int_{T}^{3T} \left(\frac{n R T}{V}\right) \times \left(\frac{d T}{2kV}\right)$$

$$= \int_{T}^{3T} \frac{n R T d T}{2 k V^{2}}$$

$$= \frac{n R}{2} \int_{T}^{3T} dT \quad (\because kV^{2} = T)$$

$$= n R T$$

51 (b)

Work done $(P\Delta V)$ = area under the (P - V)curve, which is the largest for curve 3 and the smallest for curve 1

52 (d)

In adiabatic process

$$\Delta Q = 0$$

Therefore, first law of thermodynamics becomes

$$dU + dW = 0$$

53 (c) For a diatomic gas $C_p = \frac{7R}{2}$ and $C_v = \frac{5R}{2}$ $\Delta Q = n C_p \Delta T = \frac{7}{2} nR\Delta T$ $\Delta U = n C_{\nu} \Delta T = \frac{5}{2} nR\Delta T$ From the first law of thermodynamics $\Delta W = \Delta Q - \Delta U = \frac{7}{2} n R \Delta T - \frac{5}{2} n R \Delta T$ $= n R \Delta T$ $\therefore \Delta Q : \Delta U : \Delta W = 7 : 5 : 2$ 54 (c) $\frac{W}{Q} = 1 - \frac{T_2}{T_1} = 1 - \frac{300}{600} = 0.5$ Therefore Q = 2W $= 2 \times 800 = 1600$ J :)

 $W_{A \to B}$ = Area of $ABED = \frac{1}{2}BC \times AC + CD \times DE$ $=\frac{1}{2}(6 \times 10^{-3} \text{m}^3) \times 4 \text{ Nm}^{-2} + 4 \text{ Nm}^{-2} \times 6$ $\times 10^{-3} m^{3}$ = 0.012 + 0.024 = 0.036 J $W_{B \to C}$ = Area of *BCDE* = -0.024 J. The negative sign shows that the work is done on the gas $W_{C \to A} = P \Delta V = 0$ because $\Delta V = 0$ Work done in complete cycle = 0.036 - 0.024 + 0= 0.012 J 56 **(a,c)** Since W_2 and W_3 are negative, it means that the work is done on the gas. Hence Q_2 and Q_3 are negative which implies that heat is evolved in processes 2 and 3. Since Q_1 and Q_4 are positive, heat I absorbed by the gas in processes 1 and 4. As $(Q_1 + Q_4)$ is greater than $(Q_2 + Q_3)$, the gas absorbs a net amount of heat energy in a complete cycle, which is given by $\Delta Q = Q_1 + Q_2 + Q_3 + Q_4$ = 5960 - 5585 - 2980 + 3645= 1040 joule The net work done by the gas is $\Delta W = W_1 + W_2 + W_3 + W_4$ $= 2200 - 825 - 1100 + W_4$ $= (275 + W_4)$ joule Since the process is cyclic, the change in internal energy $\Delta U = 0$. From the first law of thermodynamics, We have $\Delta W = \Delta Q - \Delta U = \Delta Q$ Or $275 + W_4 = 1040$ or $W_4 = 1040 - 275$ = 765 IEfficiency of the cycle is defined as net work done by the gas $h = \frac{1}{\text{total heat absorbed by the gas}}$ $=\frac{\Delta W}{Q_1+Q_4}=\frac{275+765}{5960+3645}$ $=\frac{1040}{9605}=0.1083=10.83\%$ $\simeq 11\%$ 57 (a,b,c,d) Along all the three paths, volume of gas is

increasing.

Therefore, heat is absorbed by the gas in all the three paths. As ΔU is independent of path, change in internal energy of the gas is same along all the three paths.

As area under path 1 is maximum therefore ΔW is maximum in path 1.

 $\Delta Q = (\Delta U + \Delta W) \text{ must be maximum in path 1}$ 58 **(a,c,d)** (a) $PV = nRT \Rightarrow n = \frac{PV}{RT}$ $= \frac{(1.6 \times 10^6) \times 0.0083}{8.3 \times 300} = \frac{16}{3}$ (b) For a monoatomic gas $C_p = \frac{5R}{2} = \frac{5}{2} \times 8.3$ $= 20.75 \text{ J mol}^{-1} \text{K}^{-1}$ (c) $\Delta Q = n C_v \Delta T; C_v = \frac{3R}{2}$ $\therefore \Delta T = \frac{\Delta Q}{nC_v} = \frac{2\Delta Q}{3nR} = \frac{2 \times 2.49 \times 10^4}{3 \times \frac{16}{3} \times 8.3}$ = 375 K $\therefore \text{ Final temperature} = 300 + 375 = 675 \text{ K}$

$$(a)_{T_2}^{P_2} = \frac{P_1}{T_1} \Rightarrow P_2 \frac{P_1 \times T_2}{T_1} = \frac{1.6 \times 10^6 \times 675}{300}$$

 $= 3.6 \times 10^{6} \text{ Pa}$

59 **(a,b,c)**

 $\Delta W = P\Delta V$ and $\Delta U = nC_v\Delta T$ and $\gamma = C_p/C_v$. Also $\Delta Q = \Delta U + \Delta W$ For an isothermal process, $\Delta T = 0$. Therefore $\Delta U = 0$. Hence $\Delta Q = \Delta W$, which is choice (a). For an adiabatic process $\Delta Q = 0$. So $\Delta U = -\Delta W$, which is choice (b). For an isochoric process, $\Delta W = 0$, so $\Delta Q = \Delta U$, which is choice (c). For an isobaric process, $\Delta Q = \Delta U + \Delta W$. So choice (d) is wrong

60 **(d)**

For adiabatic changes, $pV^{\gamma} = \text{constant}$ $P\left(\frac{RT}{P}\right)^{\gamma} = \text{constant}$ $\therefore P^{1-\gamma}T^{\gamma} = \frac{\text{constant}}{R_{\gamma}}$ another constant

61 **(a,c)**

For adiabatic process, $PV^{\gamma} = \text{constant.}$ Differentiating w.r.t *V* we get $\frac{dP}{dV}V^{\gamma} + P\gamma V^{\gamma-1} = 0$ Or $\frac{dP}{dV} = -\frac{\gamma P}{V}$ For isothermal process, PV = constant. Hence $\frac{dP}{dV} = -\frac{P}{V}$ Now, dP/dV is the slope of the (P - V)graph. Thus the slope of the (P - V) graph for an adiabatic process is γ times that for an isothermal process. Hence curves *BC* and *DA* both represent adiabatic process and curves *AB* and *CD* both represent isothermal process. Thus the correct choices are (a) and (c)

62 **(a,b)**

Isothermal curve from *A* to *B* will be parabolic with lesser area under the curve than the area under straight line *AB*. Therefore, work done by the gas in going straight from *A* to *B* is more. Temperature (a) in correct

If p_0 , V_0 be the intercepts of curve on p and V axes, then its equation is obtained from y = mx + c

$$ie \ p = \frac{p_0}{V_0}V + p_0$$

or
$$\frac{RT}{V} = \frac{p_0V}{V_0} + p_0$$

or
$$T = \frac{p_0}{V_0R}V^2 + \frac{p_0V}{R}$$

Which is the equation of a parabola. Hence T - V curve is parabolic. Therefore (b) is correct.

Also $(p/2) \times (2V) = pV = \text{constant } ie \text{ process is}$ isothermal

63 **(a,b,c)**

The internal energy of n moles of an ideal gas at absolute temperature T is given by

 $U = nC_v T \tag{1}$

Where C_v is the molar specific heat at constant volume. We know that

$$C_p - C_v = R \text{ or } \frac{C_p}{C_v} - 1 = \frac{R}{C_v}$$

Or $\gamma - 1 = \frac{R}{C_v} \text{ or } C_v = \frac{R}{\gamma - 1}$ (2)

Now, the ideal gas equation for n nodes is

$$PV = nRT \text{ or } n \frac{PV}{RT} \quad (3)$$

Using (2) and (3) in (1), we have
$$U = \frac{PV}{RT} \times \frac{R}{\gamma - 1} \times T = \frac{PV}{(\gamma - 1)}$$

64 (a,b,c,d)

All the four choices are correct

65 **(b,c)**

For an adiabatic change the relation between T and V is

$$TV^{(\gamma-1)} = \text{constant}; \gamma = \frac{C_p}{C_v}$$

$$TV^{(\gamma-1)} = T'V'^{(\gamma-1)} \text{ or } \left(\frac{V'}{V}\right)^{(\gamma-1)} = \frac{T}{T'}$$

Given $V' = 5.66$ V and $T' = \frac{T}{2}$. Therefore,
 $(5.66)^{(\gamma-1)} = 2$
Taking logarithm of both sides, we have
 $(\gamma - 1) \log(5.66) = \log(2)$

Or $\gamma = 1 + \frac{\log(2)}{\log(5.66)} = 1 + \frac{0.3010}{0.7528}$ = 1 + 0.4 = 1.4

Since $\gamma = 1.4$, the gas is diatomic. For a diatomic gas, the number of degrees of freedom of the molecules = 5

We know that the work done by the gas during adiabatic expansion is given by

$$W = \frac{1}{(\gamma - 1)} (PV - P'V') \quad (1)$$

Where pressure P' after expansion I obtained from the relation

$$\frac{P'V'}{T'} = \frac{PV}{T}$$
Or $P' = P \times \frac{V}{V'} \times \frac{T'}{T}$

$$= P \times \frac{V}{5.66V} \times \frac{T/2}{T} = \frac{T/2}{T} = \frac{P}{11.32}$$
Putting $\gamma = 1.4, V' = 5.66 V$ and $P' = \frac{P}{11.32}$ in
In Eq. (1), we have
$$W = \frac{1}{(1.4 - 1)} \left(PV - \frac{P}{11.32} \times 5.66V \right)$$

$$= \frac{1}{0.4} \left(PV - \frac{1}{2} PV \right) = 1.25 PV$$

So the correct choices are (b) and (c)

66 **(a,b,c,d)**

In an adiabatic process, $pV^{\gamma} = \text{constant}$ As $V \propto \frac{1}{\rho}$ $\therefore \frac{p}{\rho^{\gamma}} = \text{constant}$ As $p = \frac{RT}{V}$, $\therefore \left(\frac{RT}{V}\right) \times V^{\gamma} = \text{constant or } TV^{\gamma-1} = \text{constant}$ As $V = \frac{RT}{p}$, $\therefore p\left(\frac{RT}{p}\right)^{\gamma} = \text{constant or } \frac{T^{\gamma}}{p^{\gamma-1}} = \text{constant}$ All the four choices are correct

67 **(a,b,d)**

(a) Work done in process A to B is (see fig.) W_1 = area of trapezium ABCD

$$= \left(P + \frac{P}{2}\right)V = \frac{3 PV}{2}$$
$$= \frac{3 RT}{2} \text{ (for 1 mole)}$$



If the process *A* to *B* were isothermal, the work done would be

$$W_2 = RT \log_e \left(\frac{V_2}{V_1}\right) = RT \log_e(2) = 0.69 RT$$

Thus $W_1 > W_2$. So choice (a) is correct (b) Let P_0 and V_0 be the intercepts on the *P* and *V* axes. The equation of straight line *AB* is

$$P = -\frac{P_0}{V_0}(V - V_0)$$

$$\Rightarrow \frac{P}{P_0} + \frac{V}{V_0} = 1$$
(1)

Since $P = \frac{RT}{V}$, Eq. (1) becomes

$$\frac{RT}{VP_0} + \frac{V}{V_0} = 1 \Rightarrow T = \frac{P_0V}{R} - \frac{P_0V^2}{RV_0}$$

Which represents a parabola on the *T*-*V* graph So choice (b) is also correct

(c) Since $V = \frac{RT}{R}$, Eq. (1) becomes

$$\frac{P}{P_0} + \frac{RT}{PV_0} = 1 \Rightarrow T = V_0 P - \frac{V_0 P^2}{RP_0} \quad (2)$$

Which does not represent a hyperbola. So choice (c) is incorrect

(d) If follows from Eq. (2) above that choice (d) is correct

68 **(b,c)**

There is a decrease in volume during melting of an ice slab at 273*K*. Therefore, negative work is done by ice-water system on the atmosphere or positive work is done on the ice-water system by the atmosphere. Hence option (b) is correct. Secondly heat is absorbed during melting (*i. e.* ΔQ is positive) and as we have seen, work done by ice-water system is negative (ΔW is negative). Therefore, from first law of thermodynamics $\Delta U = \Delta Q - \Delta W$

Change in internal energy of ice-water system, ΔU will be positive or internal energy will increase

69 **(a,b,c,d)**

(a)Heat extracted from water is $Q_2 = mL = 10^3 \times 80 = 80,000 \text{ J} = 80,000 \times 4.2 = 3.36 \times 10^5 \text{ J}$. So choice (a) is correct

(b) $\beta = \frac{T_2}{T_1 - T_2} = \frac{273}{300 - 273} \simeq 10$. Choice (b) is correct

(c) $W = \frac{Q_2}{\beta} = \frac{3.36 \times 10^5}{10} \simeq 3.36 \times 10^4$ J, which is choice (c)

(d)
$$Q_1 = Q_2 + W = 3.36 \times 10^5 + 3.36 \times 10^4$$

 $\approx 37 \times 10^4 \text{ J}$

Power $= \frac{Q_1}{t} = \frac{37 \times 10^4 \text{J}}{180 \text{s}} \simeq 20 \text{ kW}$. So choice (d) is also correct

70 (a,b,d)

(a) $T_2 = 27^{\circ}\text{C} = 300$ K, efficiency $\eta = 0.25$ $\eta = 1 - \frac{T_2}{T_1} \Rightarrow 0.25 = 1 - \frac{300}{T_1}$ which gives $T_1 = 400$ K. So choice (a) is correct (b) Increase in efficiency = 20% of 0.25=0.05. So new efficiency is $\eta' = 0.25 + 0.05 = 0.30$. The new temperature of the source should be T'_1 so that

$$0.30 = 1 - \frac{T_2}{T_1'} = 1 - \frac{300}{T_1'}$$

Which gives $T'_1 = 428.6$ K. So, increase in temperature of the source $= T'_1 - T_1 = 428.6 - 400 = 28.6$ K or °C. So choice (b) is also correct (c) The new temperature T'_2 of the sink should be such that

$$0.30 = 1 - \frac{T_2'}{T_1} = 1 - \frac{T_2'}{400}$$

Which gives $T'_2 = 280 \text{ K} = 7^{\circ}\text{C}$. Decrease in temperature of the sink is $27^{\circ}\text{C} - 7^{\circ}\text{C} = 20^{\circ}\text{C}$, Choice (c) is wrong (d) Work output = $Q\eta = 800 \times 0.25 = 200 \text{ J}$

71 **(b,d)**

Oxygen is diatomic; it has 5 degrees of freedom. Therefore, $C_v = 5 R/2$ and $C_p = 7 R/2$. So $\gamma = C_p/C_v = 7/5$. The kinetic energy of oxygen molecules with a velocity $v_0 = \frac{1}{2} Mv^2$, where M =molecular weight of oxygen Now heat energy $= C_v dT = C_v \times 1 = C_v$ But $C_p - C_v = R$ or $\frac{C_p}{C_v} - 1 = \frac{R}{C_v}$ Or $(\gamma - 1) = \frac{R}{C_v}$ or $C_v = \frac{R}{(\gamma - 1)}$ Therefore, $\frac{1}{2}Mv^2 = \frac{R}{(\gamma - 1)}$ Or $v = \sqrt{\frac{2R}{M(\gamma - 1)}}$ So the correct choices are (b) and (d)

72 **(b)**

The P - V graph for an adiabatic process is not a

straight-line. Hence choice (a) is wrong. $P_A V_A = n R T_A$ and $P_B V_B = n R T_B$. Therefore $\frac{P_A V_A}{P_B V_B} = \frac{T_A}{T_B} \Rightarrow \frac{6 \times 1}{2 \times 4} \Rightarrow \frac{T_A}{T_B} = \frac{3}{4}$, i.e. $T_B > T_A$. Hence the internal energy increases. Work done = area under *AB* upto the volume axis. Heat energy is absorbed in the process

73 (b,d)

(a)*p*-*V*graph is not rectangular hyperbola. Therefore, process $A \rightarrow B$ is not isothermal.

(b)In process *BCD*, product of pV(therefore temperature and internal energy) is decreasing. Further, volume is decreasing. Hence, work done is also negative. Hence, Q will be negative or heat will flow out of the gas.

 $W_{ABC} = \text{positive}$

(d)For clockwise cycle on *p*-*V* diagram with *p* on *y*-axis, net work done is positive.

74 **(c)**

In a cyclic process, the system returns to its initial state. Hence the change in internal energy dU = 0. Therefore, choice (b) is correct. From the first law of thermodynamics,

dQ = dU + dW = dW (: dU = 0) Hence choice (c) is also correct

75 **(a,b,c)**

For point *A*, $PV = 5 \times (2 \times 10^{-3}) = 10 \times 10^{-3}$ J For point *B*, $PV = 2 \times (5 \times 10^{-3}) = 10 \times 10^{-3}$ J Since PV = constant, the process is isothermal. For an isothermal process, $\Delta U = 0$. Since the gas undergoes expansion ΔW is positive and $\Delta Q = \Delta W$.

76 **(a,b)**

$$T_A = T_B \qquad \therefore U_A = U_B$$

$$W_{AB} = (1)(R)T_0 \ln\left(\frac{V_f}{V_i}\right)$$
$$= RT_0 \ln\left(\frac{4V_0}{V_0}\right)$$

 $=p_0V_0\mathrm{In}\left(4\right)$

Information regarding *p* and *T* at *C* cannot be obtained from the given graph. Unless it is mentioned that line *BC* passes through origin or not.

Hence, the correct options are (a) and (b).

77 **(a,d)** Statements (a) and (d) are wrong. Concept of entropy is associated with second law of thermodynamics.

78 **(a,b,c,d)**

(a) $\Delta U = n C_v \Delta T$

(b) $\Delta Q = \Delta U + \Delta W$. For an adiabatic process, $\Delta Q = 0$. Hence $0 = \Delta U + \Delta W$ or $|\Delta U| = |\Delta W|$ (c) For an isothermal process, $\Delta T = 0$, Hence $\Delta U = 0$

(d) For an adiabatic process, $\Delta Q = 0$

79 (a,c,d)

As shown in figure, during the process *A* to *B*, *p* and *V* both decrease. As $T \propto pV$, therefore, *T* must also be decreasing. So must be the internal energy $\therefore \Delta U_{A \rightarrow B}$ is negative. As volume is decreasing, therefore, $\Delta W_{A \rightarrow B}$ is also negative. Thus, $\Delta Q_{A \rightarrow B} =$ negative

During the process *B* to *C*, volume is increasing at constant pressure. Therefore, $T(\propto pV)$ must increase and so does the internal energy.

 $\Delta U_{C \to A}$ = positive. During the process *CAB*, volume is decreasing. Therefore, ΔW_{CAB} = negative

(d)

As there is no change in internal energy of the system during an isothermal change. Hence, the energy taken by the gas is utilised by doing work against external pressure. According to FLOT $\Delta Q = \Delta U + P\Delta V$

Hence $\Delta Q = \Delta U + P \Delta V$; $\Delta U = 0 \therefore \Delta Q = P \Delta V$

Therefore, reason is true and assertion is false

81 **(d)**

Entropy is a measure of the disorder or randomness of the system. Greater the randomness, greater the entropy

82 **(b)**

Efficiency of carnot cycle $\eta = \frac{W}{Q_1} = 1 - \frac{T_2}{T_1}$, for Carnot engine when T_2 decreases η increases

83 (c)

First law of thermodynamics is a restatement of the principle of conservation of energy as applied to heat energy. Assertion is true but Reason is false.

84 (a)

Here, $T_1 = 227 + 273 = 500$ K

$$T_2 = 127 + 273 = 400 \text{ K}$$

$$\eta = 1 - \frac{T_2}{T_1} = 1 - \frac{400}{500} = \frac{1}{5} = 20\%$$

This is the maximum value of efficiency. Both the Assertion and Reason are true and Reason is correct explanation of Assertion

85 **(d)**

According to first law of thermodynamics, $\Delta Q = \Delta U + \Delta W = \Delta U + P\Delta V$. If heat is supplied in such a manner that volume does not change $\Delta V = 0, i. e.$, isochoric process, then whole of the heat energy supplied to the system will increase internal energy only. But, in any other process it is not possible.

Also heat may be absorbed or evolved when state of thermal equilibrium changes

86 **(b)**

For using the internal energy of sea water, to operate the engine of a ship, the internal of the sea water has to be converted into mechanical energy. Since, whole of the internal energy cannot be converted into mechanical energy, a part has to be rejected to a colder body (sink). Since, no such body is available, the internal energy of the sea water cannot be used to operate the engine of the ship A refrigerator is a heat engine working in the reverse direction.

87 (a)

Carnot cycle has maximum efficiency

88 **(a)**

The correct choice is (a). Statement-1 is true only if the two bodies have the same thermal capacity which is equal to mass of the body \times its specific heat capacity. Since two bodies have the same mass and are made of the same material, they have the same thermal capacity.

89 (a)

The temperature of land rises rapidly as compared to sea because of specific heat of land is five times less than that of sea water. Thus, the air above the land become hot and light so rises up because of pressure drops over land. To compensate the drop of pressure, the cooler air starts blowing towards land as well as sea radiate heat energy. The temperature of land falls more rapidly as compared to sea water, as sea water consists of higher specific heat, capacity. The air above sea water being warm and light rises up. To take its place the cold air from land starts blowing towards sea and so set-up breeze.

91 (a)

The correct choice is (a). Since the two vessels are of equal capacity, the volume occupied by the gas is doubled when the stop clock is opened. Hence, pressure becomes half

92 **(d)**

According to second law of thermodynamics, this is not possible to transfer heat from a body at lower temperature to a body at higher temperature without the aid of an external agent. Since, the given information produces a contradiction in second law of thermodynamics, therefore it is not possible to produce temperature of 8000 K by collecting the sun rays with a lens

93 **(b)**

Adiabatic curve is steeper than isothermal curve. Therefore, area under adiabatic curve is smaller than the area under isothermal; curve *ie*, work done by the gas in adiabatic expansion is smaller than the work done by the gas in isothermal expansion. The reverse is also true. Reason is true. Reason is also true but Reason does not explain Assertion

98 **(a)**

As $\eta = 1 - \frac{T_2}{T_1} = \frac{T_1 - T_2}{T_2}$, therefore, η will decrease if $(T_1 - T_2)$ decreases

Both, the Assertion and Reason are true and latter is correct explanation of the former

99 **(c)**

In an adiabatic process, no exchange of heat is permissible, i. *e*., $\Delta Q = 0$

As, $\Delta Q = \Delta U + \Delta W = 0 \Rightarrow \Delta U = -\Delta W$

Also in adiabatic process, temperature of gas changes

101 (a)

In reversible process, there always occurs some loss of energy. This is because energy spent in working against the dissipative force is not recovered back. Some irreversible process occurs in nature such as friction where extra work is done to cancel the effect of friction. Salt dissolves in water but a salt does not separate by itself into pure salt and pure water

102 **(a)**

$$\eta = 1 - \frac{T_2}{T_1} = 1 - \frac{100}{400} = \frac{3}{4} = 75\%$$

Both, the Assertion and Reason are true and Reason is correct explanation of Assertion

103 **(b)**

When milk cools, its energy content decreases

104 **(d)**

In adiabatic process, there is no exchange of heat bet6ween the system and the surroundings. This can be possible if the gas under adiabatic process is allowed to expand or compressed very quickly. Thus, it is a quick process.

When the gas is compressed adiabatically, the heat produced cannot escape to the surroundings through the insulating walls. As a result, the temperature of the gas and hence, the internal energy increase.

105 **(a)**

When a bottle of cold carbonated drink is opened a slight fog forms around the opening. This is because adiabatic expansion of gas causes lowering of temperature and condensation of water vapours

106 **(a)**

The correct choice is (a). The line *AB* is parallel to the *P*-axis. This means that PV/T is a constant, independent of pressure. Hence line *AB* corresponds to an ideal gas for which PV/T = constant. At higher temperatures, a real gas behaves more like an ideal gas. Hence T_1 is greater than T_2

107 **(d)**

As isothermal processes are very slow and so the different isothermal curves have different slopes so they cannot intersect each other

108 **(a)**

Adiabatic expansion produces cooling

109 **(d)**

We can change the temperature of a body without giving (or taking) heat to (or from) it. For example in an adiabatic compression temperature rises and in an adiabatic expansion temperature falls, although no heat is given or taken from the system in the respective changes

110 **(d)**

To carry out isothermal process, a perfect gas is compressed or allowed to expand very slowly.

Isothermal curves never intersect each other as they have very little slope

111 **(c)**

In an ideal gas, we assume that intermolecular force are zero. No work is done in charging the distance between the molecules. Therefore, internal energy is only kinetic and not potential. Therefore, internal energy of an ideal gas depends only on temperature and not on volume. Assertion is true. Reason is false.

112 **(d)**

If an electric fan is switched on in a closed room, the air will be heated because due to motion of the fan, the speed of air molecules will increase. In fact, we feel cold due to evaporation of our sweat

113 **(d)**

Zeroth law of thermodynamics explains the concept of temperature. According to which there exists a scalar quantity called temperature which is property of all thermodynamic system

114 **(a)**

Change in entropy, $\Delta S = \frac{\Delta Q}{T}$. In an adiabatic change, $\Delta Q = 0$

 $\therefore \Delta S = 0 \therefore S = \text{constant } ie$, entropy remains constant, or it is an isotropic process. Choice (a) is correct

115 **(b)**

First law of thermodynamics tells only about the conversion of mechanical energy into the heat energy and vice-versa. It does not put any condition as to why heat cannot flow from lower temperature to higher temperature.

First law of thermodynamics given

dQ = dU + dW

If heat is supplied as such its volume does not change ie, dV=0, then whole of the heat energy supplied to the system will increase in its internal energy only.

116 **(a)**

The correct choice is (a). Since the system is thermally insulated from the surroundings, no heat flows into the system or out of it, i.e. $\Delta Q = 0$. Since $\Delta U = 0$; $\Delta W = 0$

117 **(a)**

 $c = \frac{\Delta Q}{m.\Delta \theta}$; a gas may be heated by putting pressure, so it can have values for 0 to ∞

 C_P and C_V are it's two principle specific heats, out of infinite possible values

In adiabatic process C = 0, and in isothermal process $C = \infty$

118 **(a)**

Second law of thermodynamics can be explained with the help of example of refrigerator, as we know that in refrigerator, the working substance extracts heat from colder body and rejects a large amount of heat to a hotter body with the help of an external agency, i. *e.*, the electric supply of the refrigerator. No refrigerator can ever work without external supply of electric energy to it

119 **(b)**

Column -I : Expansion of ideal gas Column - II : Thermodynamic change (A) $\Delta Q = 0$ (as boundary is non conducting) in the case of free expansion W = 0 $O = \Delta U + W$ $0 = \Delta U + 0, \Delta U = 0; U = \text{constant}, T \text{ is constant}$ (A) \rightarrow (q) (As temp remains constant) (B) $P \propto \frac{1}{V_2}$ $PV^2 = C$: PV = nRTTV = CSince volume increases then temperature decreases. $Q = n C \Delta T$, for polytropic process, $PV^x =$ constant, $C = C_v + \frac{R}{1 - x}$ $C = C_v + \frac{R}{-2+1} = C_v - R \Rightarrow \frac{3}{2}R - R \Rightarrow C = \frac{R}{2}$ $\Rightarrow Q = n \frac{R}{2} \Delta T$

 ΔT is negative so Q is negative means heat is lost (B) \rightarrow (p,r)

(C) $PV^{4/3} = C, TV^{1/3} = C'$

So when volume increases then temperature decreases

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Now C = C_v + \frac{R}{\frac{4}{-2}+1} = \frac{3}{2}R - 3R \Rightarrow C = -\frac{3}{2}R
       Q = nC\Delta T \Rightarrow Q = n\left(-\frac{3}{2}R\right)(\Delta T)
       As \Delta T is negative Q will be positive
       Hence (C) \rightarrow p,s
       (D) T = \frac{PV}{nR} as product of P and V increases, so
       temperature increases Q = \Delta U + W
       \Delta U = +ve \ (\Delta T = +ve)
       W = +ve (As volume increases)
       So Q = +ve
       Hence gas gains heat (D) \rightarrow (q,s)
120 (a)
       In process \mathbf{J} \rightarrow \mathbf{K} : V is constant where as P is
       decreasing
       Therefore, T should also decrease
       \therefore W = 0, \Delta U = -ve \text{ and } Q < 0
       In process K \rightarrow L : P is constant while V is
       increasing
       Therefore, temperature should also increase
       \therefore W > 0, \Delta U > 0 and Q > 0
       In process L \rightarrow M: This is inverse of process
       J \to K
       \therefore W = 0, \Delta U > 0 \text{ and } Q > 0
       In process M \rightarrow J:
       V is decreasing. Therefore, W < 0
       (PV)_I < (PV)_M
       \therefore T_I < T_M
       \operatorname{Or} \Delta U < 0
       Therefore, Q < 0
121 (c)
       A \rightarrow B \Rightarrow V \downarrow P \ const \Rightarrow T \downarrow U \downarrow (p), (r), (t)
       B \rightarrow C \Rightarrow d\omega \downarrow 0
       P \downarrow T \downarrow
       d\phi = du + d\omega (p), (r)
       C \to D \Rightarrow V \uparrow \Rightarrow T \uparrow
       du \Rightarrow +ve
       d\omega = +ve
                         (q), (s)
       D \rightarrow A \Rightarrow d\omega \Rightarrow -ve (r), (t)
       dq \Rightarrow -ve
       du = 0
122 (c)
       Here, T_1 = 27^{\circ}C = (27 + 273)K = 300K
      T_2 = -73^{\circ}\text{C} = (-73 + 273)\text{K} = 200\text{K}
      \gamma = 1 - \frac{T_2}{T_1} = 1 - \frac{200}{300} = \frac{1}{3} = 33\%
123 (a)
```

As compression is sudden, changes are adiabatic, dQ = 0. Therefore, work done gas increases the temperature

124 **(c)**

During isothermal process $A \to B, P \propto \frac{1}{V}$. During isobaric process $(B \to C), P$ =constant and during isochoric process $(C \to A), V$ =constant. Hence the correct P - V diagram of the complete process is (c)

125 (d)

For isobaric process $A \to B$, $\frac{V_A}{T_A} = \frac{V_B}{T_B} \Rightarrow V_B = \frac{V_A T_B}{T_A} = \frac{V \times 4T/3}{T} = \frac{4V}{3}$

126 **(b)**

 $T_1 = 300 \text{ K}, V_1 = V, V_2 = 2\sqrt{2} \text{ V}$ Let T_2 be the final temperature of the gas. T_2 is obtained from the adiabatic relation

$$T_1 V_1^{(\gamma-1)} = T_2 V_2^{(\gamma-1)}$$

Or $T_2 = T_1 \times \left(\frac{V_1}{V_2}\right)^{(\gamma-1)}$

For a monoatomic gas $\gamma = \frac{5}{3}$. Therefore

$$T_2 = 300 \times \left(\frac{1}{2\sqrt{2}}\right)^{2/3} = 150 \text{ K}$$

127 (a)

Number of moles of helium is $n = \frac{\text{mass in gram}}{\text{Molecular mass}} = \frac{2000}{4} = 500$ From equation state at *A*, $P_A V_A = n R T_A \Rightarrow T_A = \frac{P_A V_A}{nR}$ $= \frac{4.15 \times 10^4 \times 10}{500 \times 8.3} = 100 \text{K}$

128 (a)

Work done by the gas in the cyclic process *ABCA* is W = area enclosed in the *P* – *V* diagram

= area of triangle
$$ABC = \frac{1}{2} \times AB \times AC$$

$$=\frac{1}{2}(3P_0 - P_0) \times (2V_0 - V_0) = P_0V_0$$

130 (c)

Using the ideal gas equation PV = nRT, the volumes of the gas in states *A*, *B* and *C* are

$$V_{A} = \frac{n RT_{A}}{P_{A}} = \frac{n R(2T_{1})}{P_{1}} = \frac{2 n RT_{1}}{P_{1}} (1)$$

$$V_{B} = \frac{n RT_{B}}{P_{B}} = \frac{n R(T_{1})}{2P_{1}} = \frac{1}{2} \frac{n RT_{1}}{P_{1}} (2)$$
and $V_{C} = \frac{n RT_{C}}{P_{C}} = \frac{n R(2T_{1})}{2P_{1}} = \frac{n RT_{1}}{P_{1}} (3)$

It is given that in the process $A \rightarrow B$, the pressure and temperature of the gas vary such that

PT = K

Where *K* is a constant. Thus for point *A*, we have $K = P_A T_A = P_1 (2 T_1)$ $= 2 P_1 T_1$ (4)

131 (c)

For process $A \rightarrow B$, the plot of *V* versus *T* is linear Hence

$$\frac{V_A}{T_A} = \frac{V_B}{T_B}$$
$$\Rightarrow T_B = \left(\frac{V_B}{V_A}\right) T_A = 2 \times 300 \text{ K} = 600 \text{ K}$$

132 (c)

Work done in $A \rightarrow B$ Isobaric process : $W = P\Delta V$ $W = \mu R\Delta T \Rightarrow W = 2 \times R \times [T_2 - T_1]$ $W = 2 \times R \times [500 - 300] \Rightarrow W = 400R$

